

Part 1: Overview of the Class

If you work hard, you will leave this class with knowledge and practical experience in three interrelated areas:

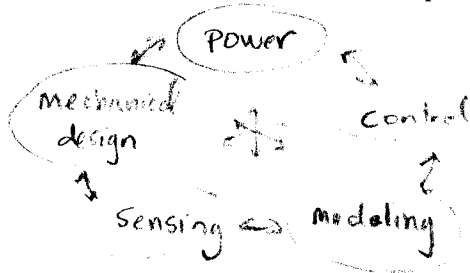
1. Physical intuition about how 1st and 2nd order linear, dynamical systems behave
 - You will be exposed to examples of common electrical, vibration, and robotic systems
 - Basic Idea: The dynamics of a wide variety of physical objects obey 1st and 2nd order linear, differential equations. These systems respond exponentially, sinusoidally, and expositoidally (OK, that's not a real word, but try to get the idea) in the time domain.
 - You will learn how to think about their behavior in both the time and frequency domains
2. Basic understanding of how feedback control works
 - Feedback is a common way to make cars, planes, robots, etc. respond like we want them too
 - You will learn about proportional feedback control (and derivative and integral control)
 - Basic idea: Measure error and try to reduce by changing the input to the controlled object
3. Familiarity with the components and tools for building mechatronic and robotic systems
 - Motors, potentiometers, tachometers, analog computational circuits (op-amps), electrical filters, power amplifiers, data acquisition systems, oscilloscopes, protoboards, ohmmeters

Part 2: Design Exercise

Final Project Competition: Build a robotic soccer player that can do two things:

1. kick a penalty kick
2. goal tend to block a penalty kick by another robot

Your robot will use a small motor. What questions do you need to know the answer to in order to build this robot?



Part 3: Review of Circuit Theory

3.1 Linear circuit elements

Current: think of it as the flow of charge through a circuit element (such as a wire or resistor) Units: amps=coulombs/sec

Voltage: think of it as the electrical pressure that can cause charge carriers to flow

Current is always measured through something at a point; voltage is always measured between two points

For this class, "ground" is an arbitrarily defined point on a circuit to which we reference all voltages

Toolbox for circuit analysis

• Kirchoff's Current Law: $\sum \text{current in} = \sum \text{current out}$

• Kirchoff's Voltage Law: $\sum_{\text{loop}} \text{voltage} = 0 \quad -V_L + V_1 + V_2 = 0$

• Power $P = VI$ (stored or dissipated)

• Triad of linear circuit elements:

	L	$\frac{di}{dt}$
V	R	L
$\frac{dv}{dt}$	C	"Flux Capacitor"

ohms (= Siemens)
 farads (filters)
 henrys (motors used to ignite spark plug in automobile engine)

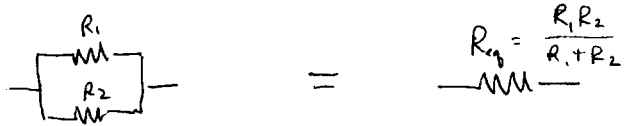
set gains (0.1 volts)

$V = L \frac{di}{dt}$

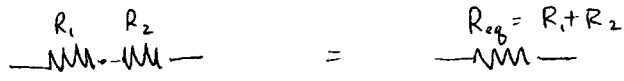
Resistor Analysis Exercise:

Abstraction: the act of considering something as a general quality or characteristic apart from any concrete realities, specific object, or actual instance. It's the idea of a "black box"

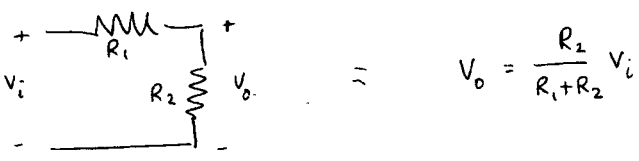
ABSTRACTION, PATTERN RECOGNITION, + CIRCUIT ANALYSIS



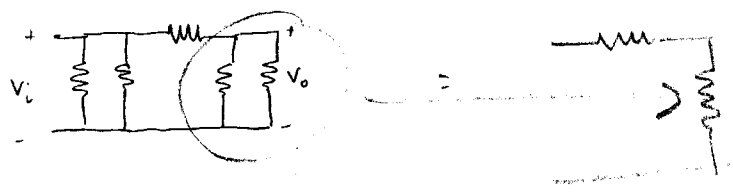
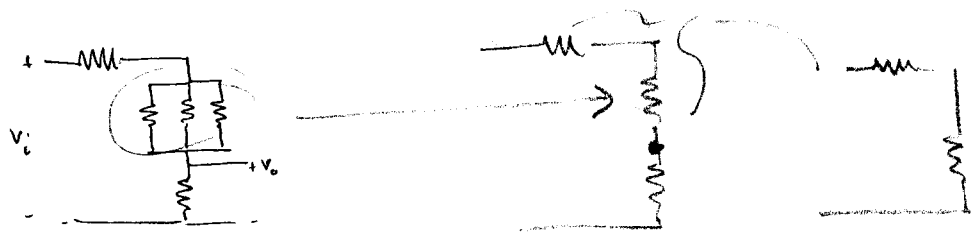
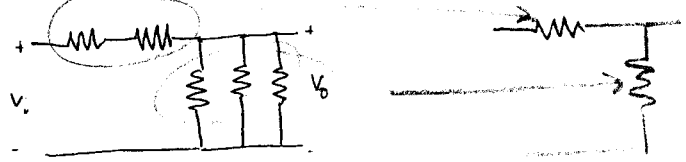
ALSO



$V = IR$
KCL
KVL

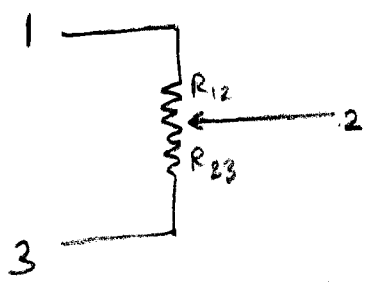
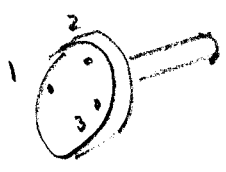


Using the above abstractions/rules, find V_o for the following circuits:



Potentiometers:

Typically used as voltage dividers. The two resistor values are changed by turning the pot.

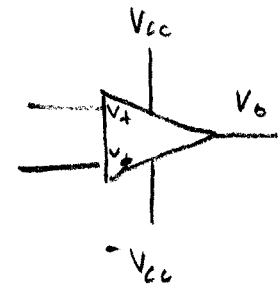


$$R = R_{12} + R_{23} = [50 \text{ k}\Omega, \text{ for example}]$$

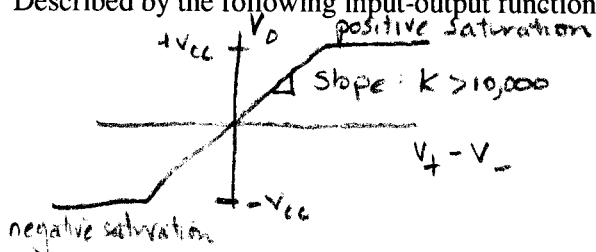
$$V_{out} = \frac{R_{23}}{R} V_{in}$$

3.2 Operational Amplifiers

- important building blocks for circuits; easy to use, cheap
- used to build filters, amplifiers, feedback controllers, computational circuits
- the "brains" in the analog control circuits that you will build for the class
- What are they? High gain, differential, linear voltage amplifiers
- Made of > 20 transistors plus resistors and capacitors
- Two input terminals, one output, two power supply lines (five pins total)
- Typically operate over a wide range of supply voltages
- By design, they have a high input resistance and a low output resistance



Described by the following input-output function:



in linear region

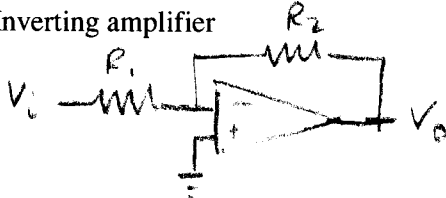
$$V_0 = K (V_+ - V_-)$$

Golden Rules of Op-amp Circuit design:

1. Input currents are zero (op amps are designed to have a high input resistance)
2. Input voltages are equal (If operating in linear region, and connected with negative feedback)

Four useful circuits:

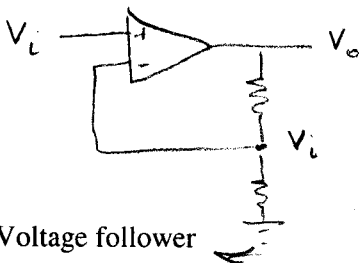
1. Inverting amplifier



What is V_0 as a function of V_i ?

$$\text{KCL: } \frac{V_i}{R_1} + \frac{V_0}{R_2} = 0 \quad V_0 = -\frac{R_2}{R_1} V_i$$

2. Non-inverting amplifier

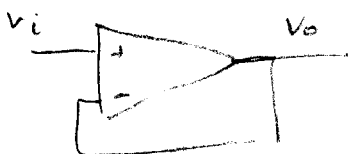


$$\frac{V_0 - V_i}{R_1} = \frac{V_i}{R_2} \Rightarrow V_0 = \frac{R_1}{R_2} V_i + V_i$$

$$V_0 = \left(\frac{R_1 + R_2}{R_2} \right) V_i$$

as $R_2 \rightarrow \infty$ what does this circuit do?

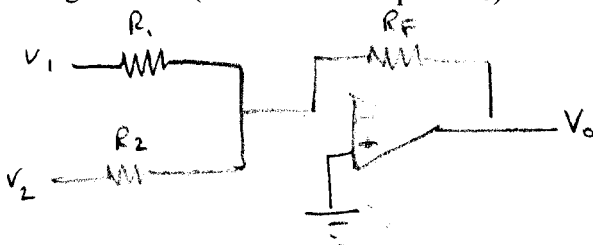
3. Voltage follower



$$V_0 = V_i$$

Why? - high input impedance lets us connect circuit modules without altering their performance

4. Analog addition (subtraction also possible)



$$\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_0}{R_F} = 0$$

$$V_0 = -R_F \left(\frac{1}{R_1} V_1 + \frac{1}{R_2} V_2 \right)$$

$$\text{If } R_1 = R_2 = R$$

$$V_0 = -\frac{R_F}{R} (V_1 + V_2)$$

Note: feedback is always to V_- (negative feedback)

$|V_0| < |V_{cc}|$ and $I_{out} < I_{max}$ else op-amp saturates

3.3 Controlling power needed for devices like motors, light bulbs, etc.

Often we want to control a device that requires a lot of power (e.g. a motor) with signals that have very low power (e.g. an op amp or computer).

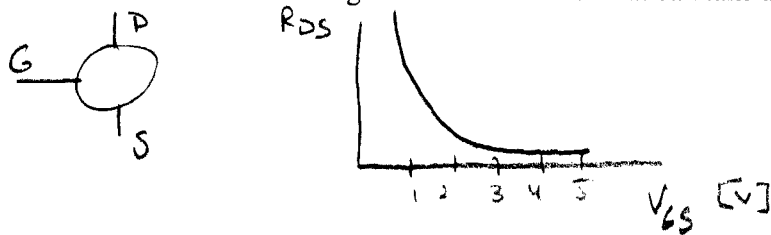
Small DC brushed motor: $V = 10\text{ V}$, $R = 2\ \Omega$ $i = \frac{V}{R} = 5\text{ amps}$

Typical Op-amp: $V = \pm 15\text{ V}$, $i_{\text{max}} < 20\text{ mA}$

Solutions?

1. Power op-amp
2. Power transistor (e.g. power MOSFET – simple and cheap)

Can think of a MOSFET as a voltage controlled resistor that can take a lot of current



Notes: Input resistance is very high (therefore effectively no current goes into gate)

Low-power MOSFETS are the “switches” used in computers (what is a switch?)

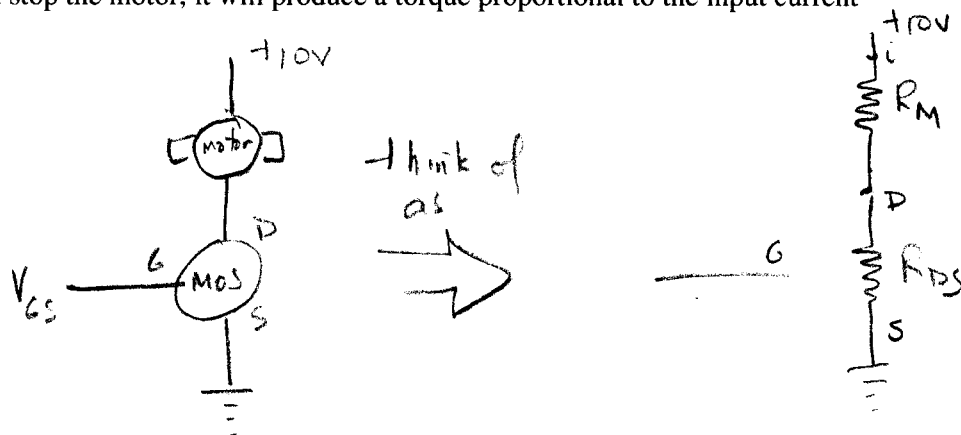
MOSFETS are very sensitive to static electricity – use a grounding strap when you handle them in lab

Example: use a power transistor to control a motor with a low-power computer output

Hints about motors:

A DC brushed motor spins at a speed proportional to the input voltage, if it is just turning an inertial load.

If you stop the motor, it will produce a torque proportional to the input current



If R_{DS} is big, no current flows

If R_{DS} is small (because V_{GS} is small) current flows

Thus, by controlling V_{GS} , we can make the motor turn or not turn

low power
no current